

Resource Allocation via the Median Rule

Clemens Puppe
joint work with Klaus Nehring

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Agenda

- 1 General Motivation
- 2 Generalized Single-Peakedness
- 3 Resource Allocation
 - Theory
 - Simulation

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- Moreover, in general, there is a large *multiplicity* of ‘insincere’ equilibria.
- **Question:** Does that mean that strategically robust implementation is impossible in economically relevant applications?

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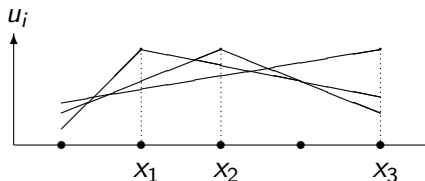
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Median Voter Theorem: *Suppose that social alternatives can be ordered from left to right such that all preferences are single-peaked, then the choice of the median of the individual peaks defines a non-dictatorial and strategy-proof voting rule.*



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Question 2: The Median Rule in Public Goods Allocation Problems

This talk

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Strategy-Proofness

- A social choice function F maps profiles of individual preferences on a (finite) set of alternatives X to a collectively chosen alternative:

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- F is **strategy-proof** if it is a (weakly) dominant strategy to submit true preference ordering: for all $\succeq_1, \dots, \succeq_n$ and \succeq'_i ,

$$F(\succeq_1, \dots, \succeq_i, \dots, \succeq_n) \succeq_i F(\succeq_1, \dots, \succeq'_i, \dots, \succeq_n)$$

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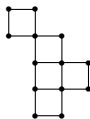
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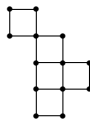
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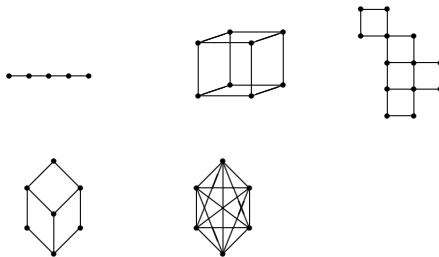
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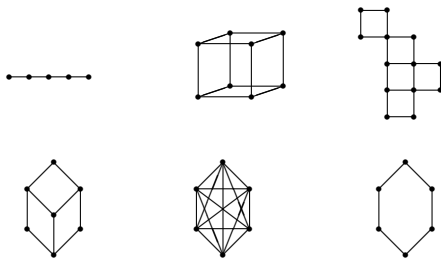
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Characterization of all strategy-proof voting rules on **all** generalized single-peaked domains:

- Betweenness-preserving embedding of graph in (high-dimensional) hypercube
- Simple game in each dimension ('voting by issues')
- Key steps:
 - 'peaks only' based on Barberá, Masso & Neme 1997
 - consistency of simple games across dimensions ('intersection property')

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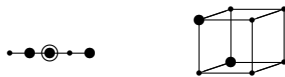
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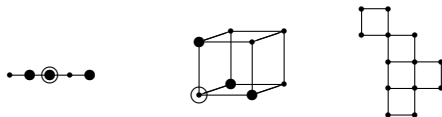
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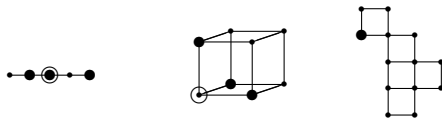
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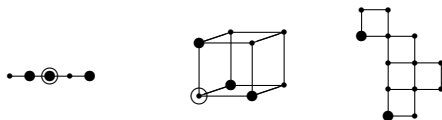
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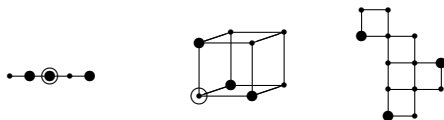
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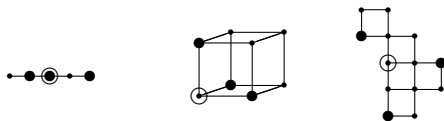
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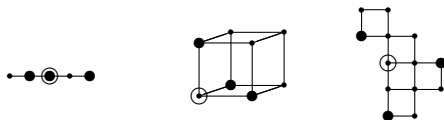
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Special cases: Moulin 1980, Demange 1982, Barberá, Sonnenschein & Zhou 1991, Barberá, Gul & Stacchetti 1993

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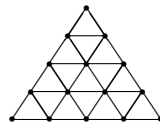
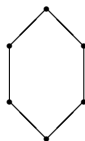
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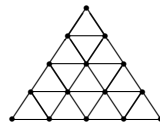
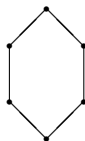
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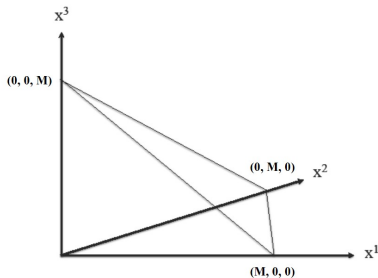
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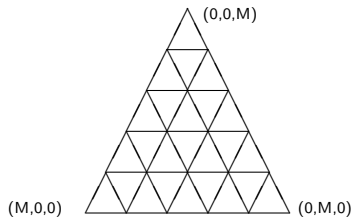
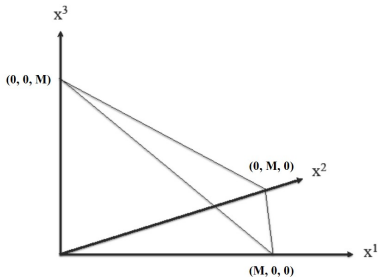
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*If $L \geq 3$, then all strategy-proof allocation mechanisms are dictatorial, **even if** one restricts the domain to sufficiently rich sets of 'generalized single-peaked' preferences (e.g. Euclidean, Cobb-Douglas, etc.).*

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Observation

*The one-dimensional median minimizes the **sum of the distances** to the individual peaks.*

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- By observation above, median rule chooses usual median if $L = 2$.
- Chooses the coordinate-wise median whenever that is feasible.
- Preference aggregation: ‘Kemeny-Young rule’ (Young & Levenglick 1978)
- In the general judgement aggregation model: Nehring & Pivato (2014a-c)

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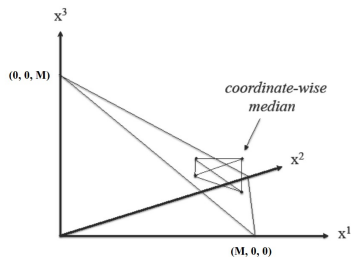
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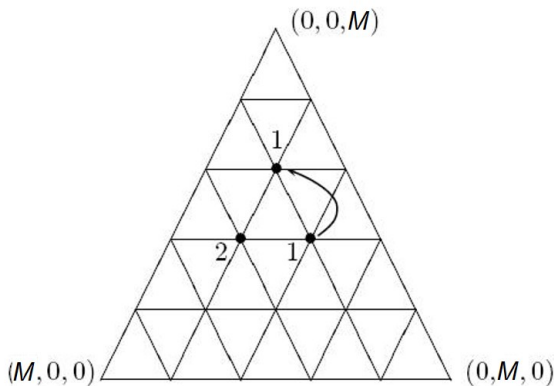
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Single-valued selections: Take any fixed allocation $\tilde{x} \in X$, and choose median allocation with minimal *Euclidean* distance to \tilde{x} .

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The (single-valued) median rule is strategy-proof on the domain of all preferences admitting a utility representation of the form $u(x) = -\|x - x^\|_1$, for some $x^* \in X$ (the peak).*

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Agenda

- 1 General Motivation
- 2 Generalized Single-Peakedness
- 3 Resource Allocation**
 - Theory
 - Simulation**

Simulation Study (with Tobias Lindner)

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- Peaks randomly drawn from Dirichlet distribution.
- Voters play myopic best response in random sequence ...
- ... under Cobb-Douglas preferences.
- Maximal 15 iterations with ...
- ... sample size 10.000.
- **Parameters:**
 - rule (mean vs. median),
 - number of voters,
 - number of goods,
 - budget size.

Simulation Study: Results

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Extent of Manipulation:

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Table: Number of agents = 5

	No. of Revisions	Max. Utility Gain	Manipulating Agents
Mean	12.11	7.41%	99.98%
Med	16.19	1,94%	59.60%

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Table: Number of agents = 45

	No. of Revisions	Max. Utility Gain	Manipulating Agents
Mean	53.09	1.87%	100.00%
Med	58.09	0.78%	39.05%

Simulation Study: Results

Effect of Manipulation

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Effect of Manipulation

Table: Number of agents = 5

	Deviation	Distance of Outcome	Welfare Loss
Mean	39.28%	7.38%	1.60%
Med	4.86%	4.51%	1.05%

Simulation Study: Results

Effect of Manipulation

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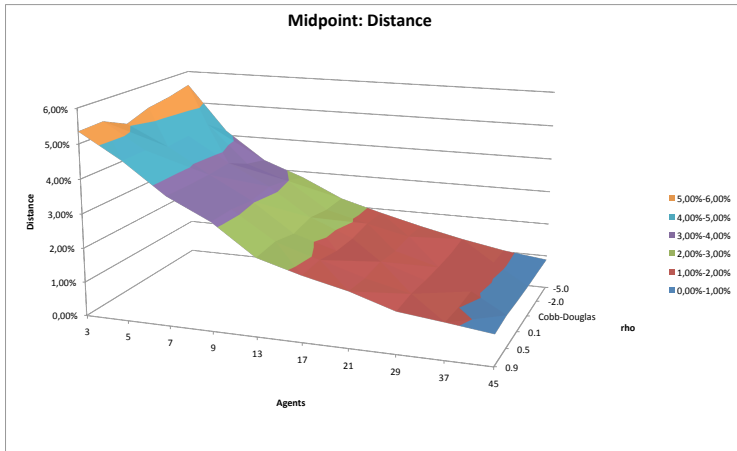
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Table: Number of agents = 45

	Deviation	Distance of Outcome	Welfare Loss
Mean	43.09%	5.73%	1.02%
Med	2.96%	0.88%	0.20%



Simulation Study: Effect of Manipulation with CES



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Thanks for your attention!!